

GENETIC ALGORITHMS: AN INTRODUCTION

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Course: Functional Programming and Intelligent Algorithms

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Topics this week

- Introduction to AI and optimisation
- Nature-inspired algorithms
 - Focus on the genetic algorithm (GA)
- Binary GAs
- Continuous GAs
- Basic applications
- Real-life case study

Recommended reading

- Main text: *Practical Genetic Algorithms*, Haupt and Haupt, 2nd Ed., 2004.
- Supplementary texts:
 - *Machine Learning: An Algorithmic Perspective*, Marsland, 2nd Ed., 2015.
 - *Artificial Intelligence: A Guide to Intelligent Systems*, Negnevitsky, 2nd Ed., 2002.
 - *Genetic Algorithms in Search, Optimization and Machine Learning*, Goldberg, 1989.
 - *Artificial Intelligence: A Modern Approach*, Russell and Norvig, 3rd Ed., 2010.

Introduction to artificial intelligence (AI)

What is AI?

- Many definitions exist
- Russell and Norvig (R&N): «*The study and design of intelligent agents*»
 - But what is an intelligent agent?
- Intelligent agent (R&N): «*a system that perceives its environment and takes actions that maximize its chances of success*»

What is AI?

- AI is a huge field involved with topics such as
 - Problem-solving
 - Knowledge, reasoning, planning
 - Uncertain knowledge and reasoning
 - Learning
 - Communicating, perceiving, acting(categories from R&N)

Tools in AI

- Search and optimisation
 - Useful in problem-solving
- Logic
- Probabilistic methods
- Classifiers and statistical learning
- Neural networks
- Control theory
- Languages

Engineering is problem-solving

- Engineering is about solving real-world problems
- Many tools available, particularly search and optimisation
- Heuristic methods useful, e.g. genetic algorithms

Some real-world problems

- Routing video streams in network
- Airline travel-planning system
- Traveling salesperson problem (TSP)
- VLSI layout problem
- Robot navigation
- Automatic assembly sequencing
- ... And million others

Introduction to optimisation

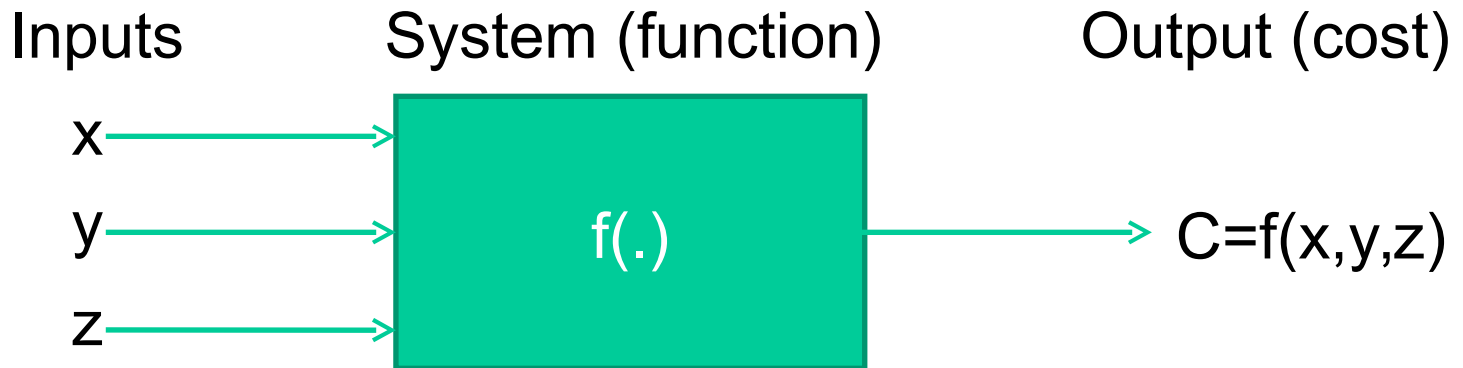
What is optimisation?

- A process of *improving* an existing idea
- Goal: Finding the *best* solution
 - What does "best" mean?
- With exact answers, "best" may have a specific definition, eg., PL top scorer
- Other times, best is a *relative* definition, eg., prettiest actress

What is optimisation?

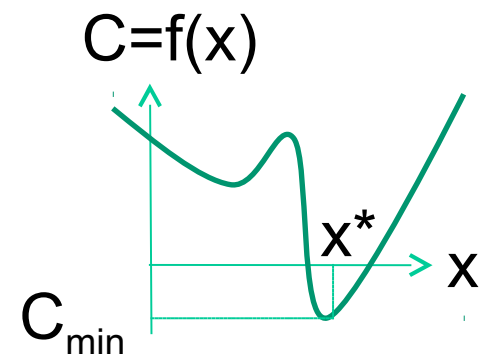
- A process of adjusting inputs to a system to find max/min output
- Inputs: Variables, e.g., x, y, z
- System: Cost function, e.g., $f(x,y,z)$
- Output: Cost evaluated at particular values of variables, e.g., $C=f(x_0,y_0,z_0)$
- Search space: Set of possible inputs, eg. all possible values of x, y, z

What is optimisation?



Q: What are the dimensions of the search space?

- Challenge: Determine optimal inputs x^*, y^*, z^* that minimises cost C .
- 1D example: $C_{\min} = f(x^*)$



Note on convention

- Optimisation is to find the minimum cost
- Equivalently, maximise fitness
- Cost function = (minus) fitness function
- Maximisation is the same as minimising the negative of the cost function (put minus in front)
- Maximising $1-x^2 \leftrightarrow$ minimising x^2-1

Root finding vs. optimisation

- Root finding: Searches for the zero of a function
- Optimisation: Searches for the zero of the function *derivative*
- 2nd derivative to determine if min/max
- Challenge: Is minimum global (optimal) or local (suboptimal)?

Categories of optimisation

- Trial and error vs. function
- Single- vs. multivariable
- Static vs. dynamic
- Discrete vs. continuous
- Constrained vs. unconstrained
- Random vs. minimum seeking

Trial and error vs. function

- Trial and error method: Adjust variables/inputs without knowing how the output will change → experimentalist approach
- Function method: Know cost function, thus may search variables/inputs in clever ways to obtain desired (optimal) output → theoretician approach

Single- vs. multivariable

- Single variable: One-dimensional (1D) optimisation
- Multivariable: Multi-dimensional (nD) optimisation
 - Difficulty increases with dimension number
- Sometimes split up nD optimisation in n series of 1D optimisations

Dynamic vs. static

- Dynamic: Output is a function of time (optimal solution changes with time)
- Static: Output is independent of time (find optimal solution once is enough)
- Example: Shortest distance from A to B in a city is static, but fastest route depends on traffic, weather, etc.

Discrete vs. continuous

- Discrete: Finite number of variable values
 - Known as combinatorial optimisation
 - Eg. optimal order to do a set of tasks
- Continuous: Variables have infinite number of possible values
 - Eg. $f(x) = x^2$

Constrained vs. unconstrained

- Constrained: Variables confined to some range
 - eg., $-1 < x < 1$
- Unconstrained: Any variable value is allowed, eg., x a real number

Minimum-seeking vs. random

- Minimum-seeking: Derivative method going downhill until reached minimum
 - Fast
 - May get stuck at local minimum
- Random: Probabilistic method
 - Slower
 - Better at finding global minimum

Minimum-seeking algorithms

Cost surface

- Cost surface consists of all possible function values
- 2D case: All values of $f(x,y)$ make up the cost surface (height = cost)
- Goal: Find minimum cost (height) in cost surface
- Downhill strategy → easily stuck in local minimum
- Can be multi-dimensional

Exhaustive search

- Brute force approach: Divide cost surface into large number of sample points.
- Check (evaluate) all points
- Choose variables that correspond to minimum
- Computationally expensive and slow

Exhaustive search

- Do not get stuck in local minimum
- May miss global minimum due to undersampling
- Refinement: First a coarse search of large cost region, then a fine search of smaller regions

Analytical optimisation

- Employ calculus (derivative methods)
- Eg., 1D case: $f(x)$ is continuous
 - Find root x_m s.t. derivative $f'(x_m)=0$
 - Check 2nd derivative
 - if $f''(x_m) > 0$, $f(x_m)$ is minimum
 - if $f''(x_m) < 0$, $f(x_m)$ is maximum
- Use gradient for multi-dim cases
 - eg., solve $\text{grad } f(x,y,z) = 0$

Analytical optimisation

- Problems:
 - Which minimum is global?
 - Must search through all found minima
 - Requires cts. diff'able functions with analytical gradients
 - Difficult with many variables
 - Suffers at cliffs or boundaries in cost surface

Well-known algorithms

- Nelder-Mead downhill simplex method
- Optimization based on line minimisation
 - Coordinate search method
 - Steepest descent algorithm
 - Newton's method techniques
 - Quadratic programming
- Natural optimisation methods